

**Calculus I**

**Name:** \_\_\_\_\_

**Study Guide 6**

**Class:** \_\_\_\_\_

**Due Date:** \_\_\_\_\_

**Score:** \_\_\_\_\_

**No Work  $\Leftrightarrow$  No Points**

**Use Pencil Only  $\Leftrightarrow$  Be Neat & Organized**

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1. (4 points) Find a value for the constant  $k$  that will make the following function continuous.

$$f(x) = \begin{cases} kx^2, & x \leq 2 \\ 2x + k, & x > 2 \end{cases}$$

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1. \_\_\_\_\_

2. (4 points) Find a value for the constant  $k$  that will make the following function continuous.

$$f(x) = \begin{cases} \frac{x^2 - 4}{x^3 - 8}, & x \neq 2 \\ k, & x = 2 \end{cases}$$

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2. \_\_\_\_\_

3. (4 points) Prove if  $f(x)$  is continuous and nonnegative, then find  $\sqrt{f(x)}$  is continuous.

3. \_\_\_\_\_

4. (4 points) Evaluate:  $\lim_{x \rightarrow a} \frac{x^6 - a^6}{x^2 - a^2}$

4. \_\_\_\_\_

5. (4 points) Evaluate:  $\lim_{x \rightarrow 0} \frac{\sin 7x}{\sin 3x}$

5. \_\_\_\_\_

6. (4 points) Evaluate:  $\lim_{x \rightarrow 3} \frac{\sin(x - 3)}{x^2 + 2x - 15}$

6. \_\_\_\_\_

7. (4 points) Evaluate  $\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$  for  $f(x) = \frac{1}{x-1}$ .

7. \_\_\_\_\_

8. (4 points) Find the equation of the tangent line to the graph of  $f(x) = x^3$  at the point  $(1, 1)$ .

8. \_\_\_\_\_

9. (4 points) Evaluate:  $\lim_{x \rightarrow \pi/2} \frac{1 - \cos(x - \pi/2)}{x - \pi/2}$

9. \_\_\_\_\_

10. (5 points) Find the equation of the normal line to the graph of  $f(x) = \sqrt{x}$  at the point  $(4, 2)$ .

10. \_\_\_\_\_

11. (4 points) Evaluate  $\lim_{x \rightarrow 0} f(x)$  if  $1 - x^4 \leq f(x) \leq \cos x$  for all  $x$  in  $[-\pi/2, \pi/2]$

11. \_\_\_\_\_

12. (5 points) For  $\epsilon = 0.1$ , find  $0 < \delta \leq 1$  such that  $\lim_{x \rightarrow 3} x^2 = 9$ .

12. \_\_\_\_\_